

Frequency-Comb Based Approaches to Precision Ranging Laser Radar

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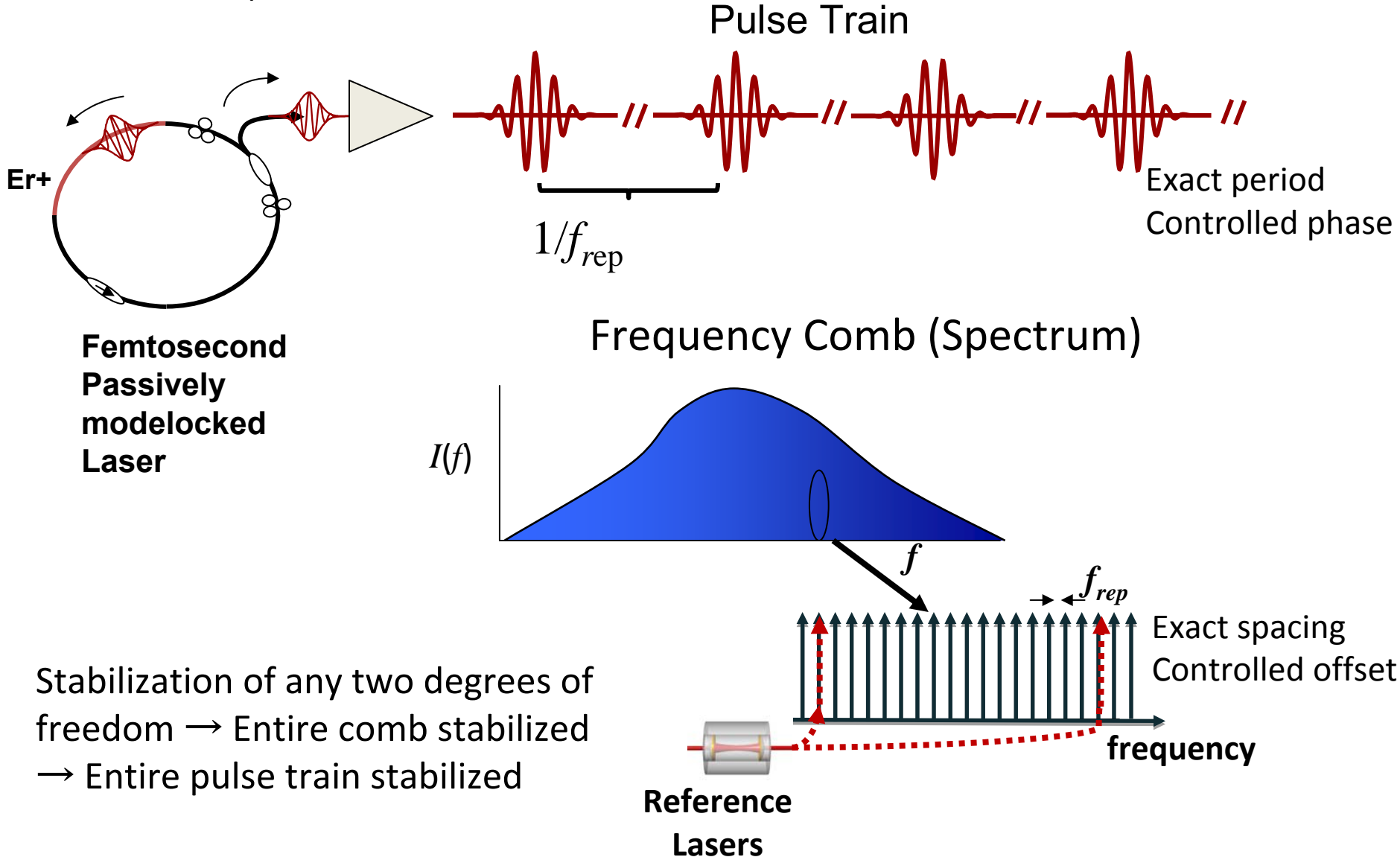
Outline

- **Introduction: Combs**
- **Combs for ranging**
- **Dual Comb ranging**
 - Initial phase-locked system: nm-level precision
 - Simplified free-running system: sub- μm precision in < 1 ms
- **Comb-assisted coherent FMCW ranging Ladar**
 - Tracking a fast swept laser
 - Preliminary results
- **Conclusion**

Frequency Comb

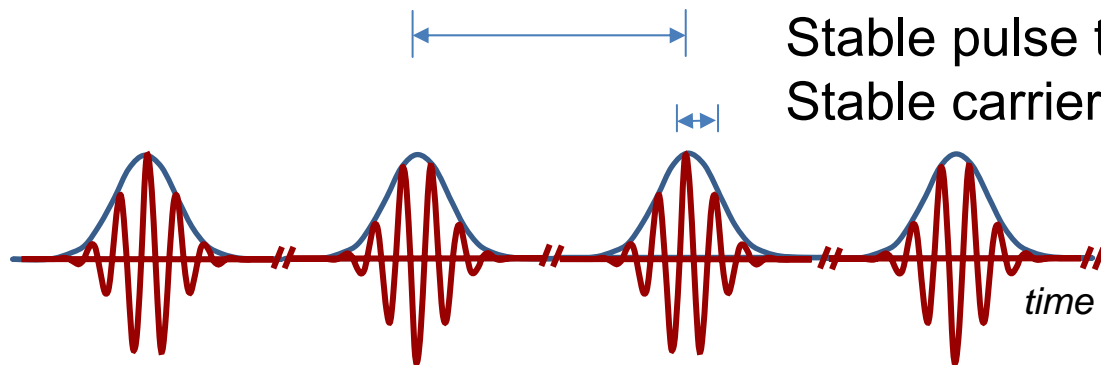
Coherent, stabilized femtosecond, mode-locked lasers

2005 Nobel prize to J. Hall & T. Hänsch



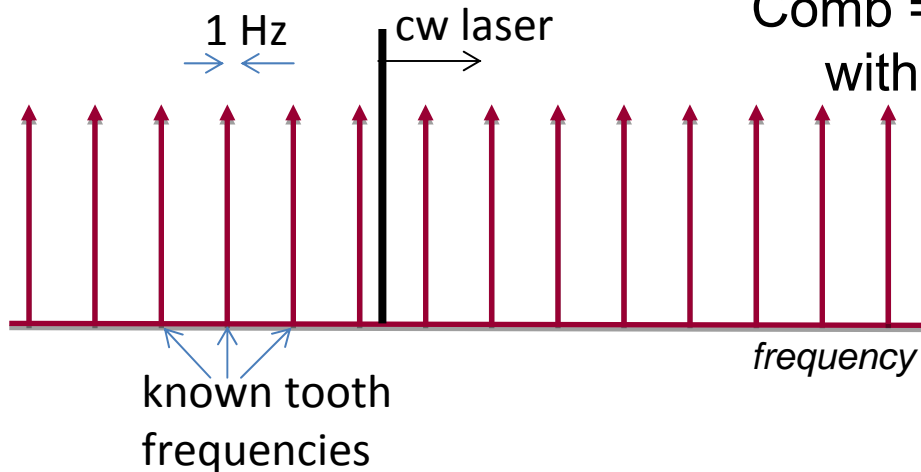
Properties of Combs For Ranging

Time-domain



Stable pulse timing → time-of-flight
Stable carrier frequency → interferometry

Frequency-domain

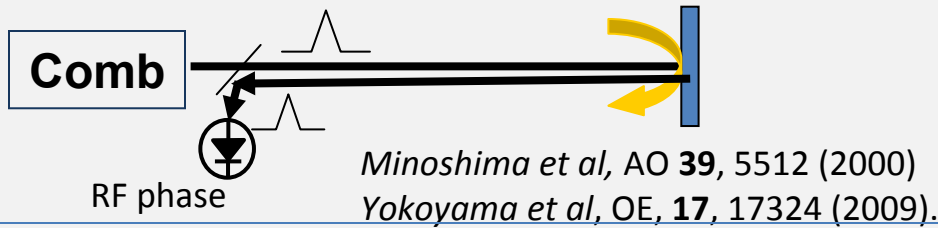


Comb = thousands to millions of “cw lasers”
with Hz-linewidths and known frequencies
→ Multi-wavelength interferometry
→ Calibration of fixed/swept lasers

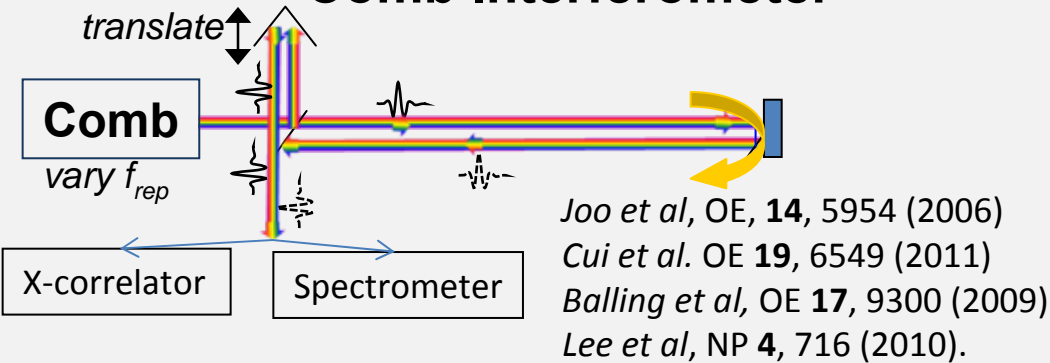
Different Comb-Based Ranging Systems

“Direct” Comb Ranging

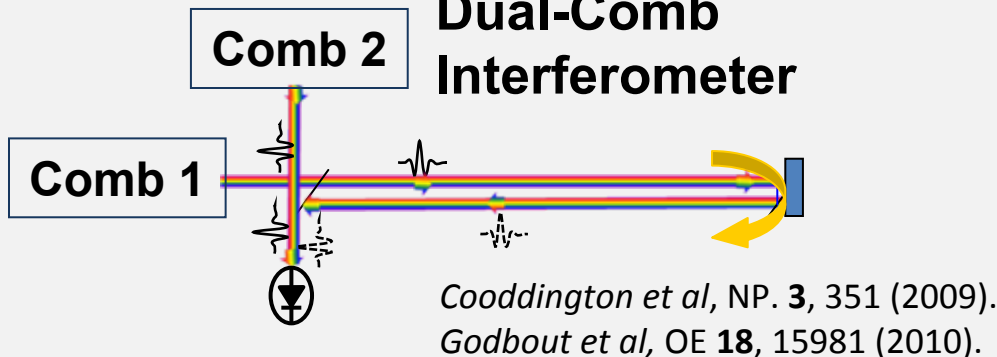
Modulated waveform



Comb Interferometer

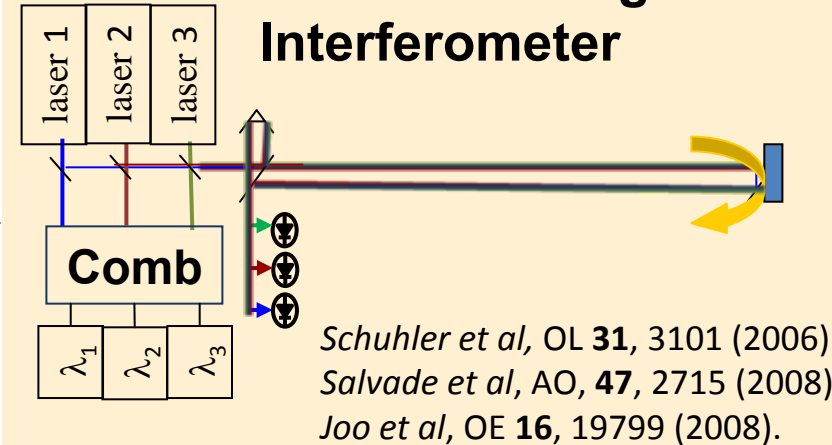


Dual-Comb Interferometer

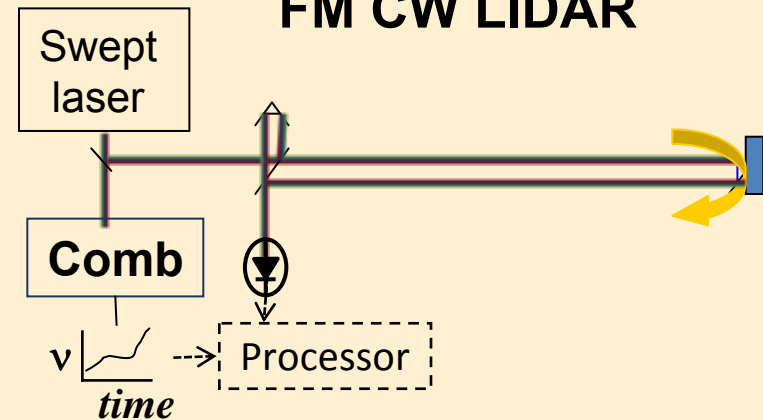


Comb-Assisted Ranging

Multi-Wavelength Interferometer



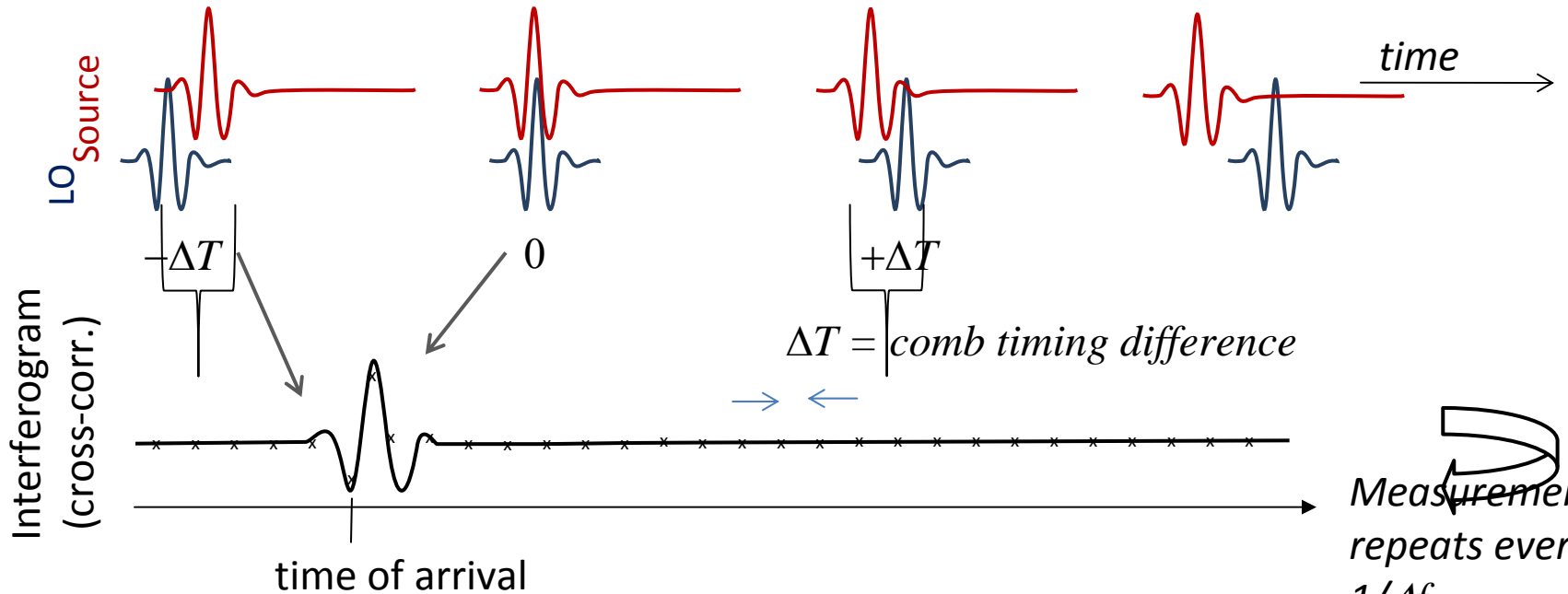
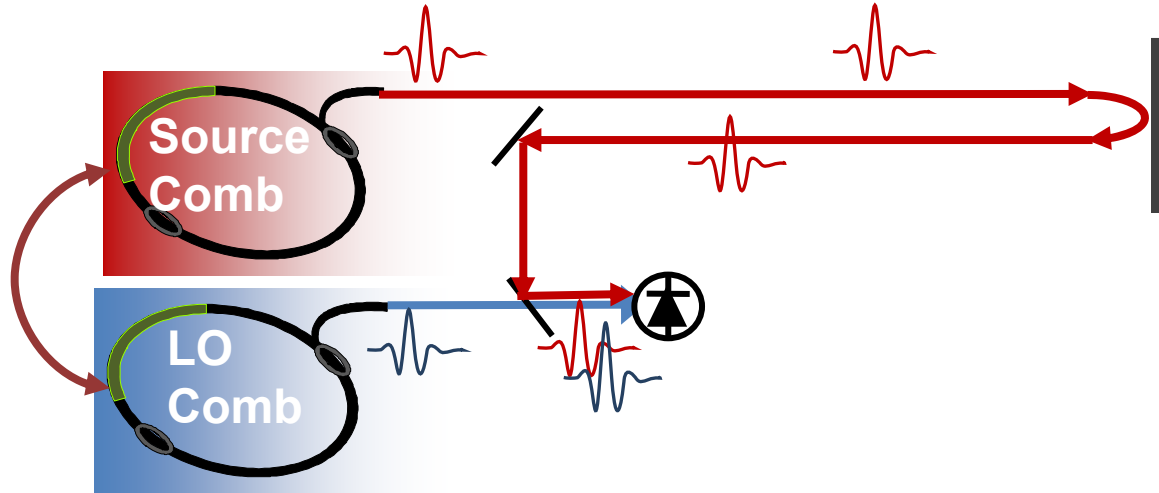
FM CW LIDAR



This work

Dual Comb System in Time Domain: Linear Optical Sampling

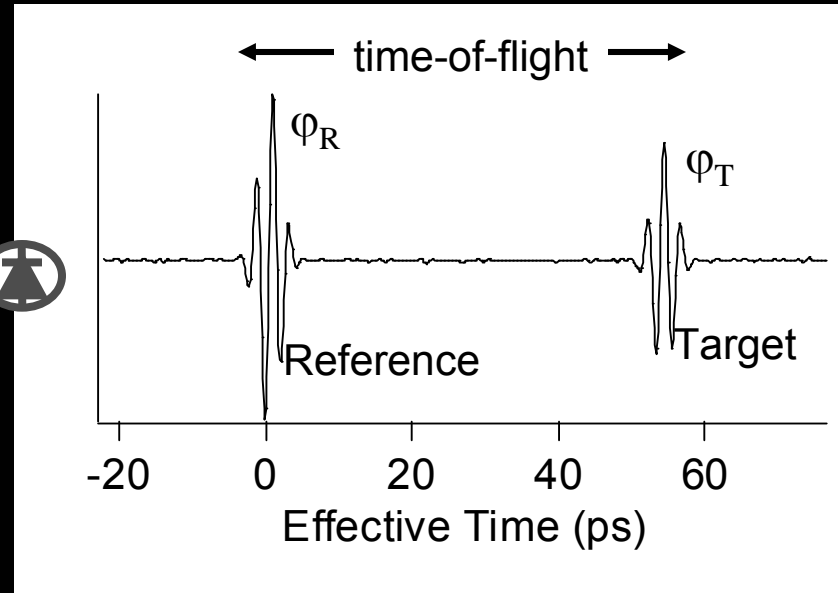
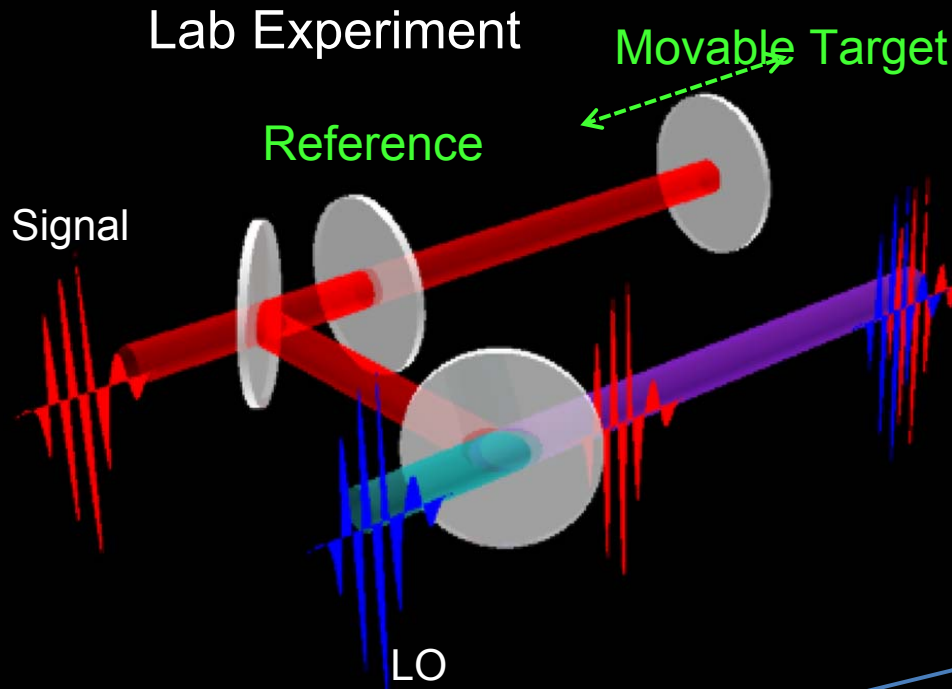
- Phaselock combs
- Coherent carrier
 - Slightly different repetition rate Δf_{rep}



A cross-correlation with timing is as precise as combs

Measurement repeats every $1/\Delta f_{rep}$

Dual-Comb Ranging: Lab Demo



Combs phase-locked together

- Coherent carrier
- Precisely offset repetition rate

Time-of-Flight Range = $(v_{\text{group}}/2) \times \text{time-of-flight}$

Absolute Range

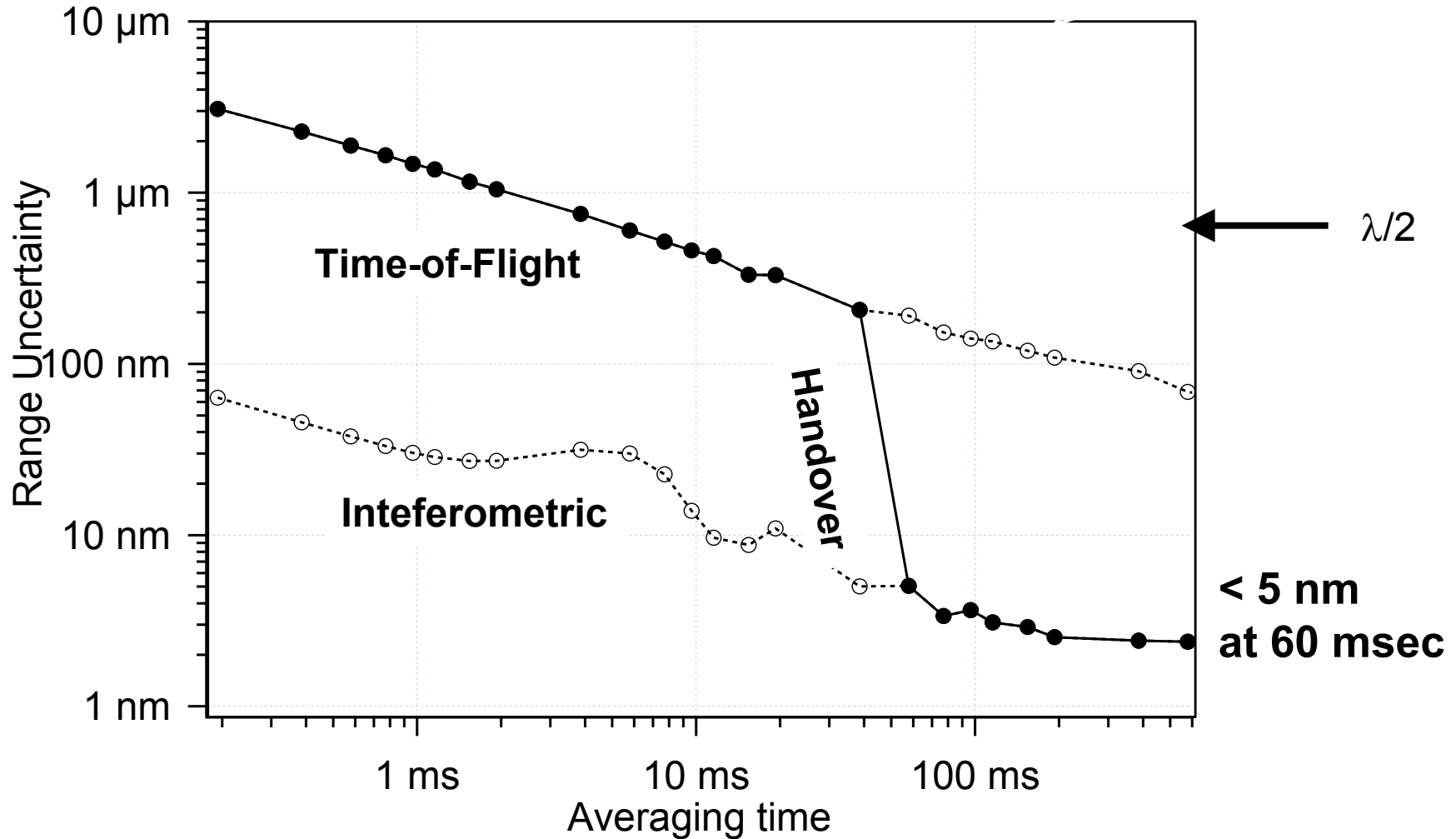
Interferometric Range = $(\phi_T - \phi_R) / (4\pi) \lambda + N \lambda/2$

High-precision Range

ambiguity

Range Uncertainty versus Observation Time nm-level absolute distance measurements

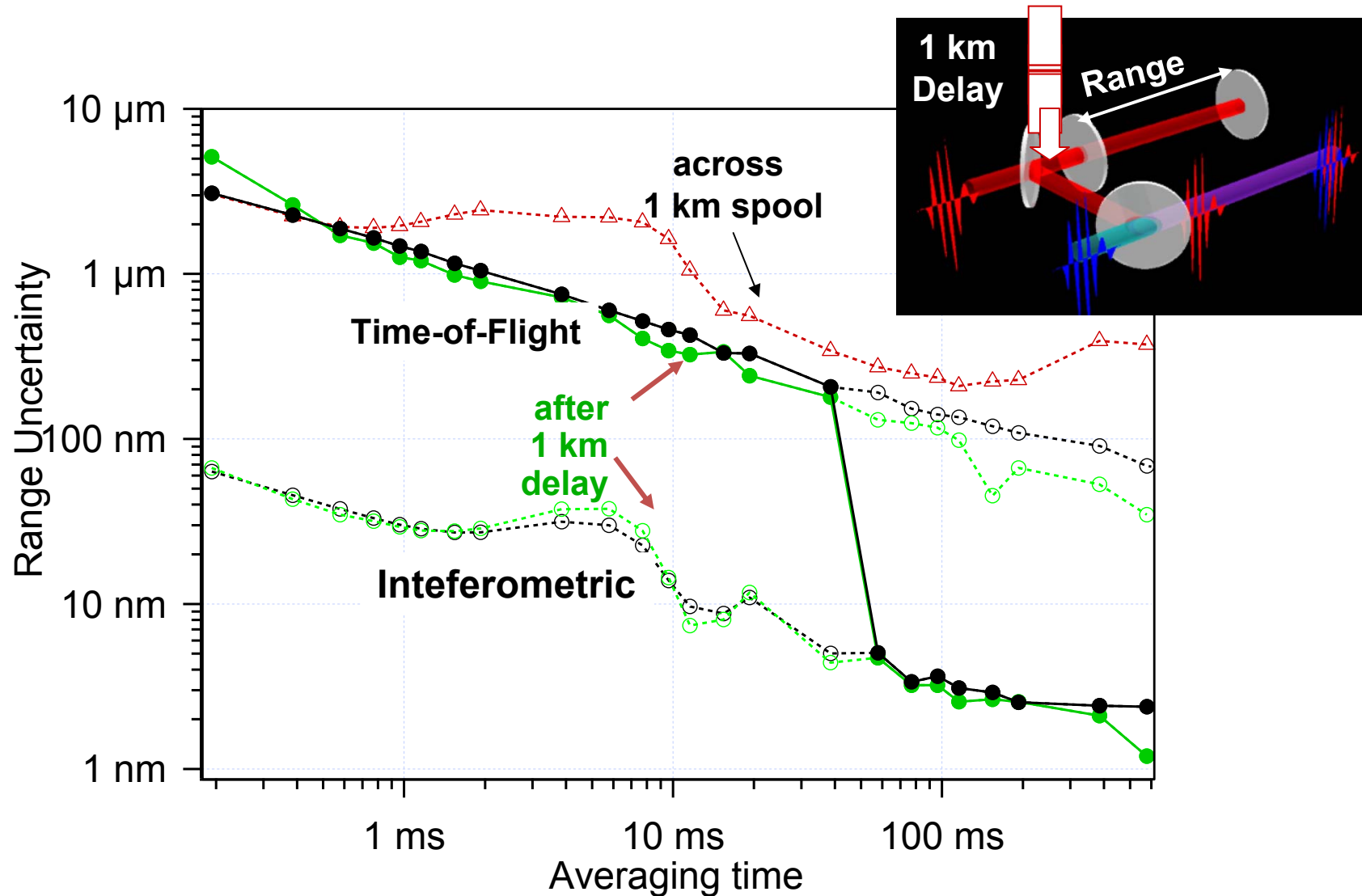
(Also verified Time-of-Flight and Interferometric Agree)



“Range Window” or Ambiguity is 1.5 meters (but can extend to > 30 km)

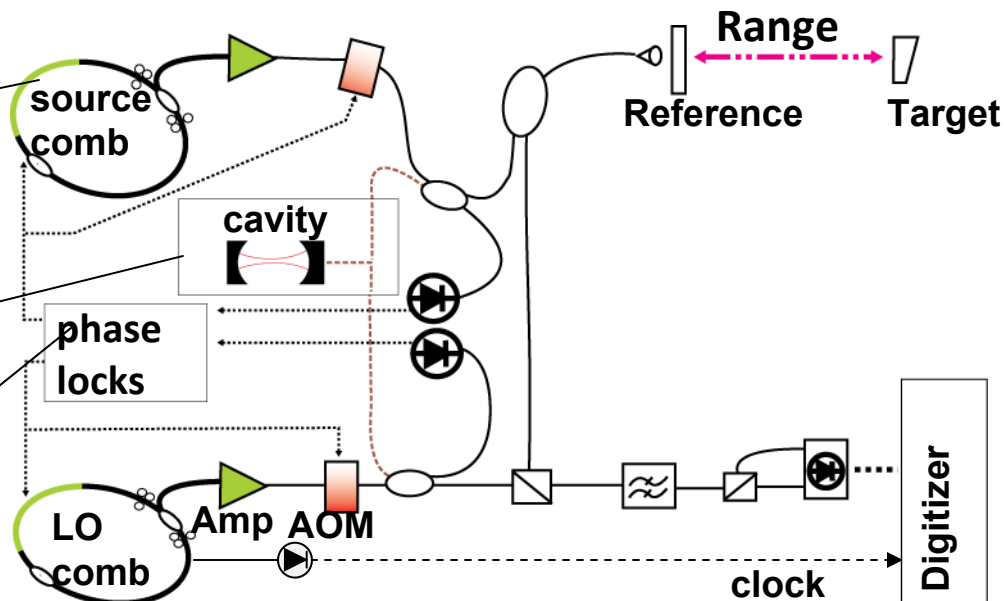
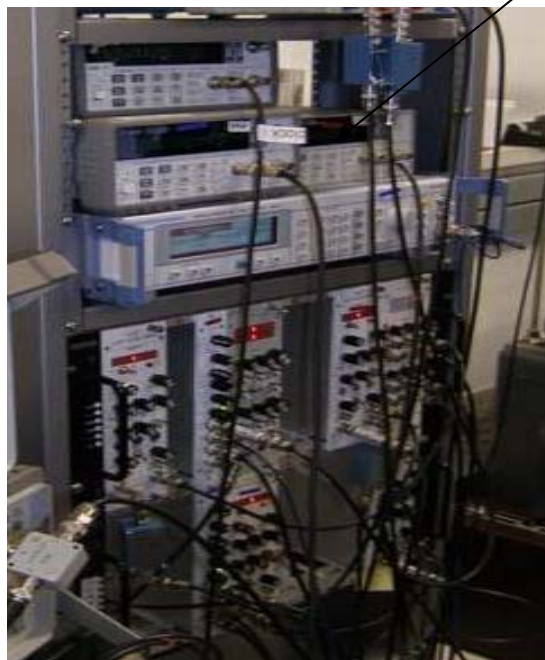
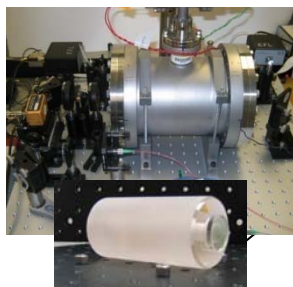
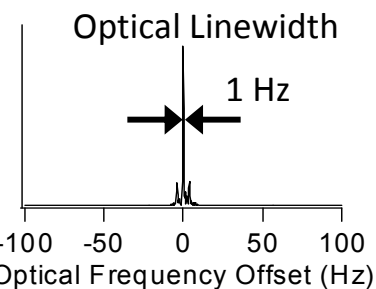
Range Uncertainty versus Observation Time

nm-level absolute distance measurements



“Range Window” or Ambiguity is 1.5 meters (but can extend to > 30 km)

Fully Phase-Locked Dual Comb System



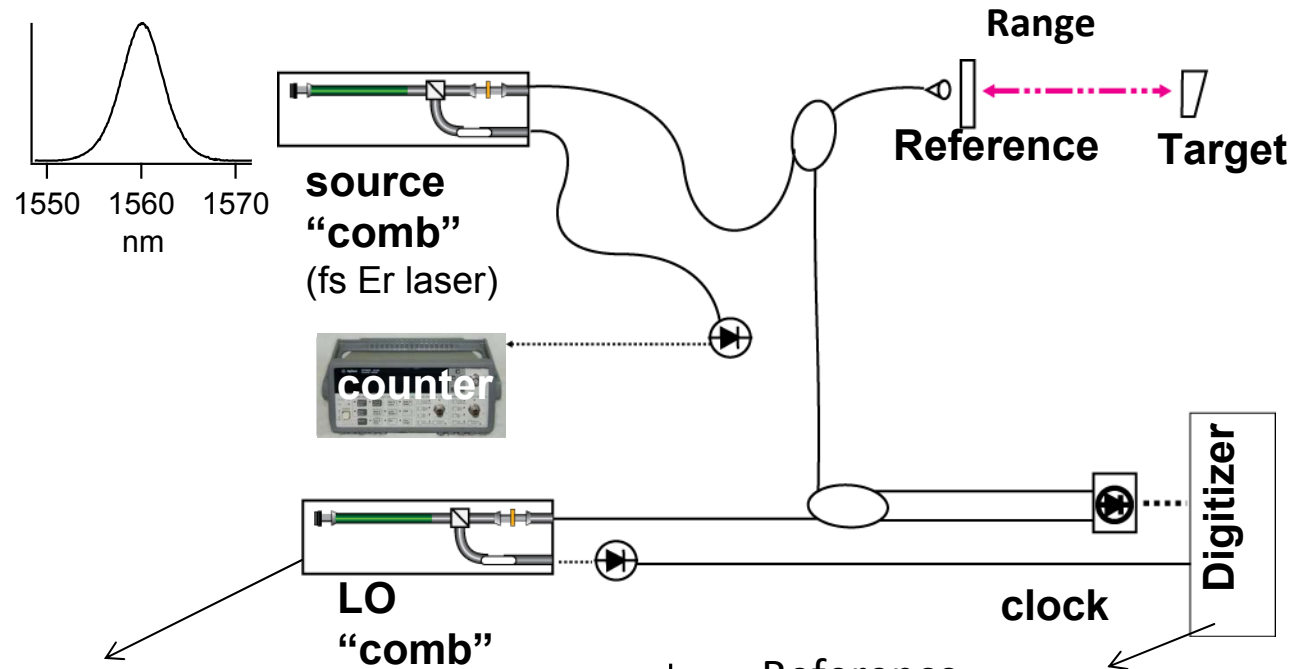
- Four phase locks to two cavity-stabilized laser
- Can we trade off precision for simplicity?
 - Nanometer precision excessive for typical terrestrial ranging of $\sim 10^{-7}$ to 10^{-8} precision

Try a free-running system with no phase locks...

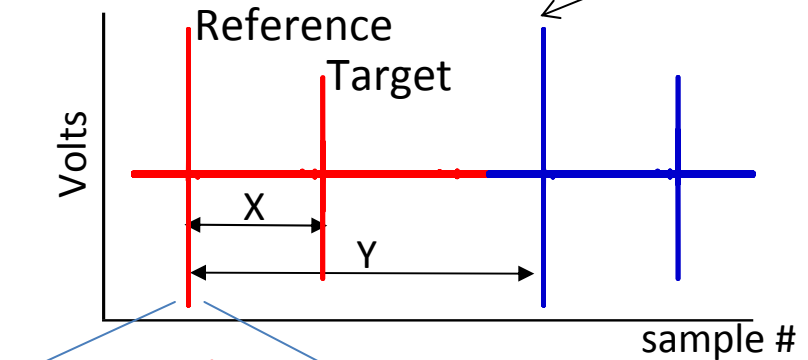
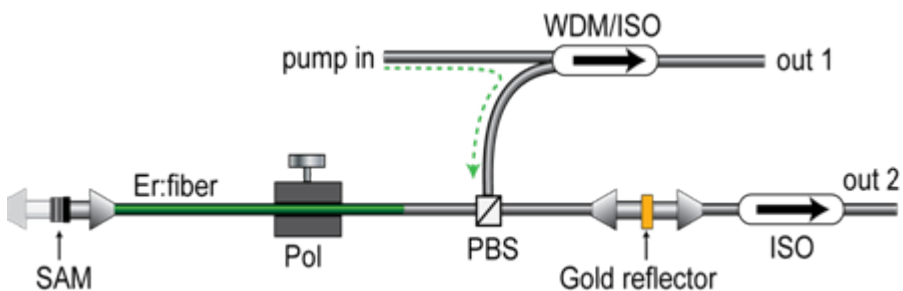
- ***Interferometric ranging lost***
- ***Time-of-flight ranging still possible?***

Free-running Dual Comb System

Time-of-Flight Ranging Without Phase Locks



Simplified 200 MHz Er fs laser



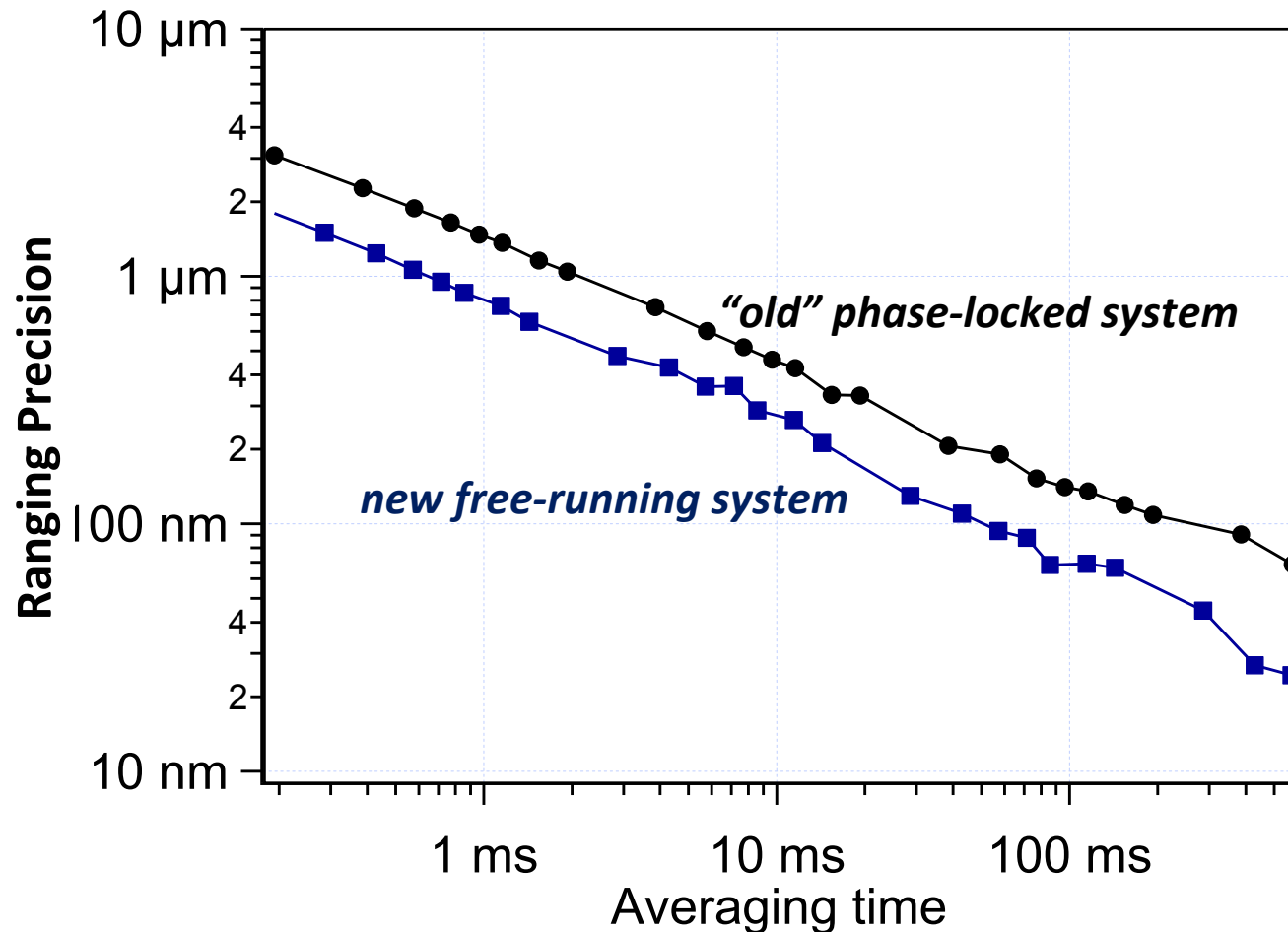
Processing

$$\frac{1}{ep} \times \frac{v_{grp}}{2}$$

Free-running rep rate stable to 10^{-8} @ 1 sec
 Adjust for $\Delta f_{rep} = 7$ kHz between combs
 Free-running carrier stable to \sim MHz

Time-of-Flight Ranging with Simpler System

Sub-micron in Sub-milliseconds with 0.75 m range window



- Superior performance (due to higher repetition rate sources)
- Also verified 200 nm linearity across 1 meter

Dual-Comb Ranging

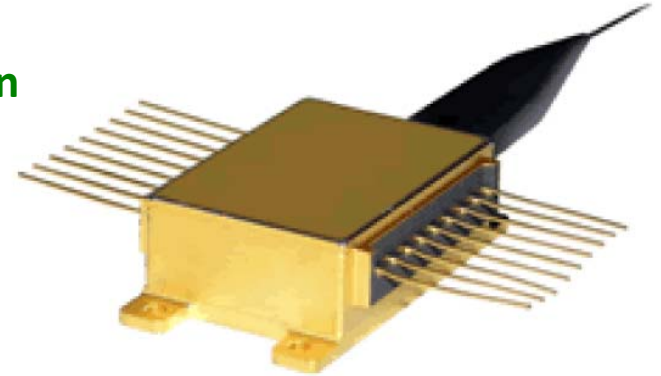
- **Advantages**
 - Rapid, absolute, high precision ranging (sub-micron in sub-millisecond)
 - Immunity to spurious reflections
 - No significant dead zones
- **Disadvantage**
 - Inefficient use of photons: Multiplexed disadvantage of \sqrt{N}
10's of nW to μ W return powers (100's of photons per pulse)
- **Suitable for ranging to “cooperative” target with retroreflector**
 - Not suitable for diffuse target
 - (True of all direct comb ranging systems....)

Can we combine accuracy of combs with efficiency of FM CW LIDAR?

Combing Swept Cw Lasers & Combs

Tunable diode lasers offer

- ~100 nm tuning ranges
- Rapid scan rates >1000 THz/s in MEMS or Y-branch design
- >10 mW - many Watts and single mode operation.
- Much higher SNR than direct-comb illumination



But

- Optical frequency is poorly defined during sweeps
(orders of magnitude worse than linewidth)
- Also fastest sweeps will not be linear (but quasi-sinusoidal)

Goal:

- Use frequency combs to track the phase of a swept laser
- ❖ With high accuracy
- ❖ At high speeds
- ❖ Over arbitrary waveforms

Metrology of a Swept CW laser using Frequency Combs

Basic Approach: Heterodyne laser against comb & digitize (fast)

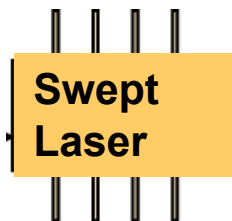
T.-A. Liu, et al. , *Opt. Exp.*, 16, 10728, (2008).

P. Del'Haye *et.al.*, *Nat. Photon.*, **3**, 529, (2009).

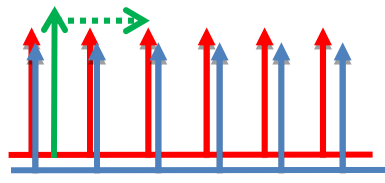
F. R. Giorgetta, *et.al.*, *Nat. Photon.*, **4**, 853, (2010)

Z. W. Barber, *et. al.*, *Opt. Lett.*, **36**, 7, 1152, (2011).

I. Coddington, *et. al.*, *JSTQE* (Invited), IEEE Early Access, (2011)

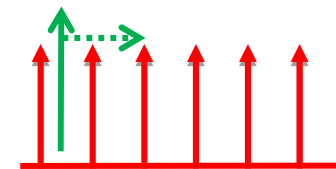


Dual Comb Spectrometer



- *Absolute* optical frequency vs time
- Requires dual phase-locked combs
- >1000x faster than wavemeter
- Unique tool for metrology of fast swept lasers

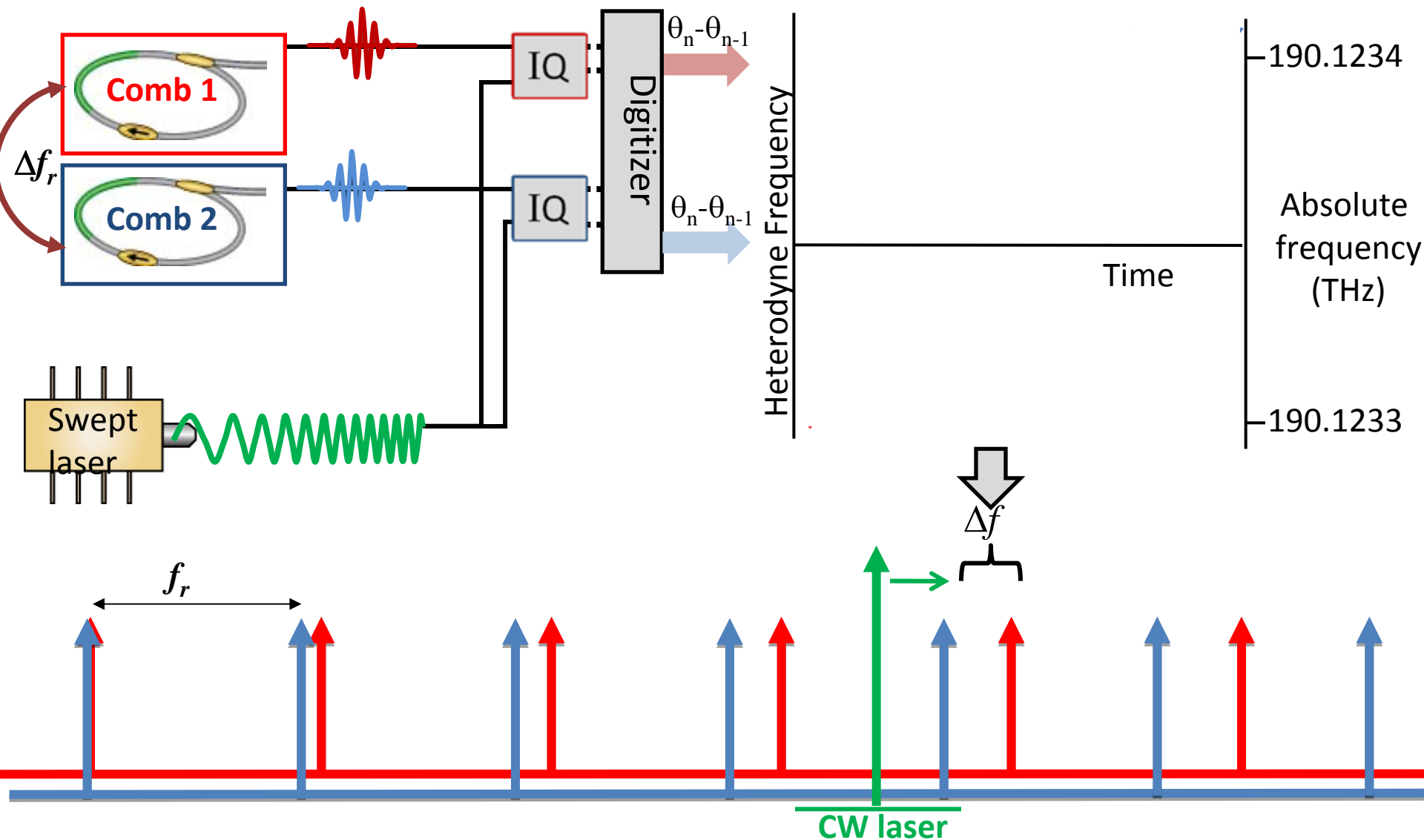
Single Comb Spectrometer



- *Relative* optical frequency vs time
- Single, free-running comb
- ~20 nanosecond time resolution
- Much higher linearity, speed, flexibility than etalon approaches

Swept CW laser + Dual Comb Spectrometer

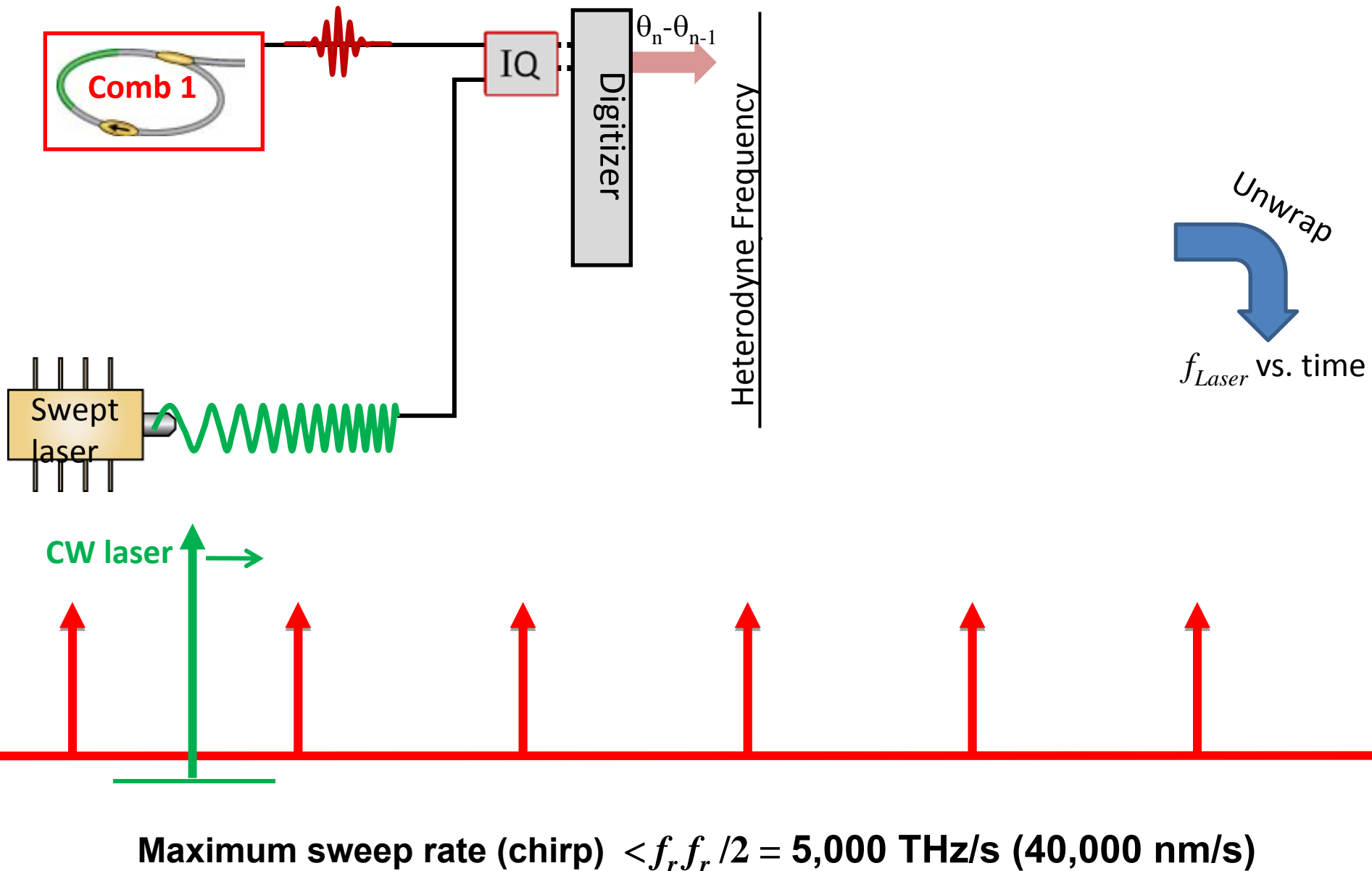
Absolute Frequency Determination



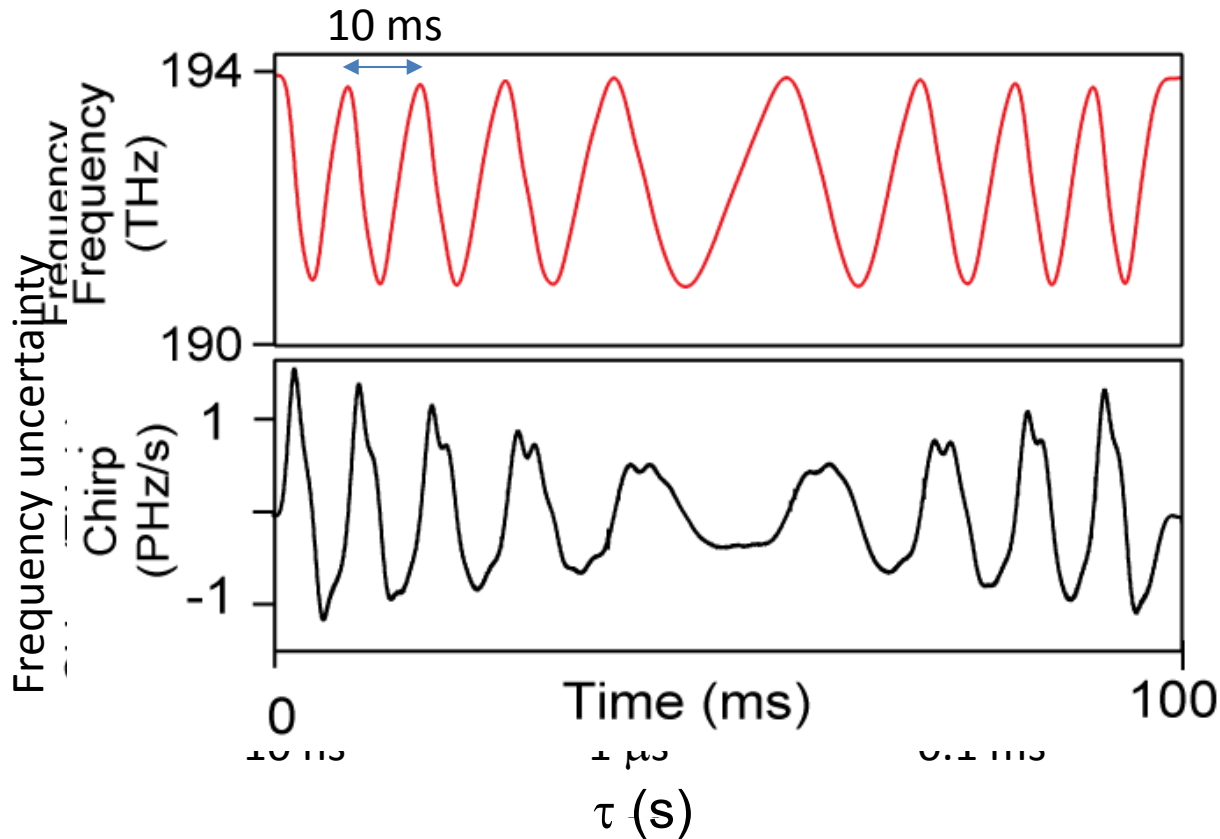
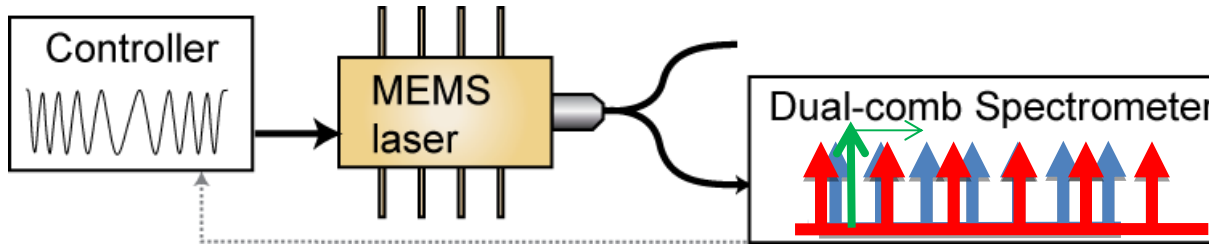
Maximum sweep rate (chirp) $< f_r \Delta f_r = 0.1-1 \text{ THz/s}$ (0.8-8 nm/s)

Swept CW laser + Single Comb Spectrometer

Fast Relative Frequency Determination



Example Measurement of a Fast Swept Laser MEMS-based ECL

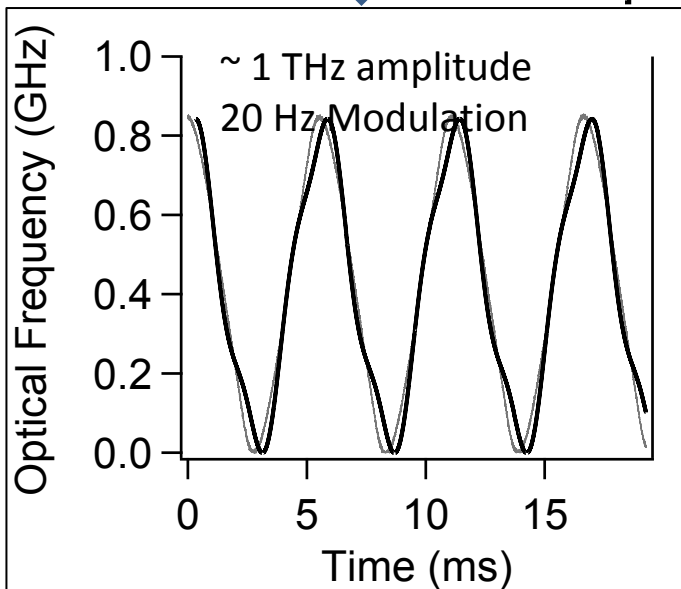
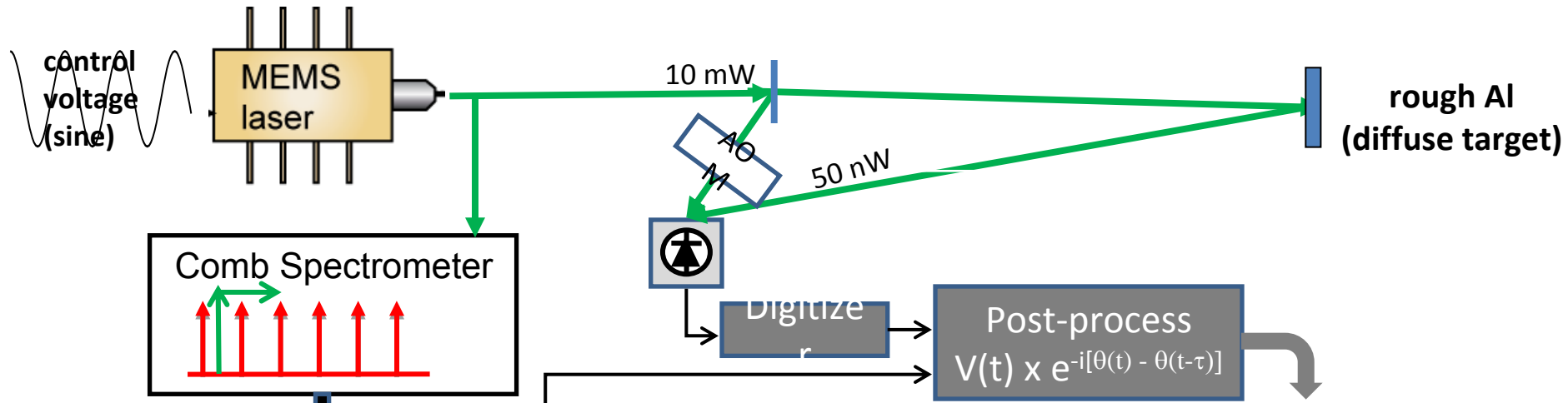


Chirp rates $> 10^{15}/\text{sec}$
(10,000 nm/sec)

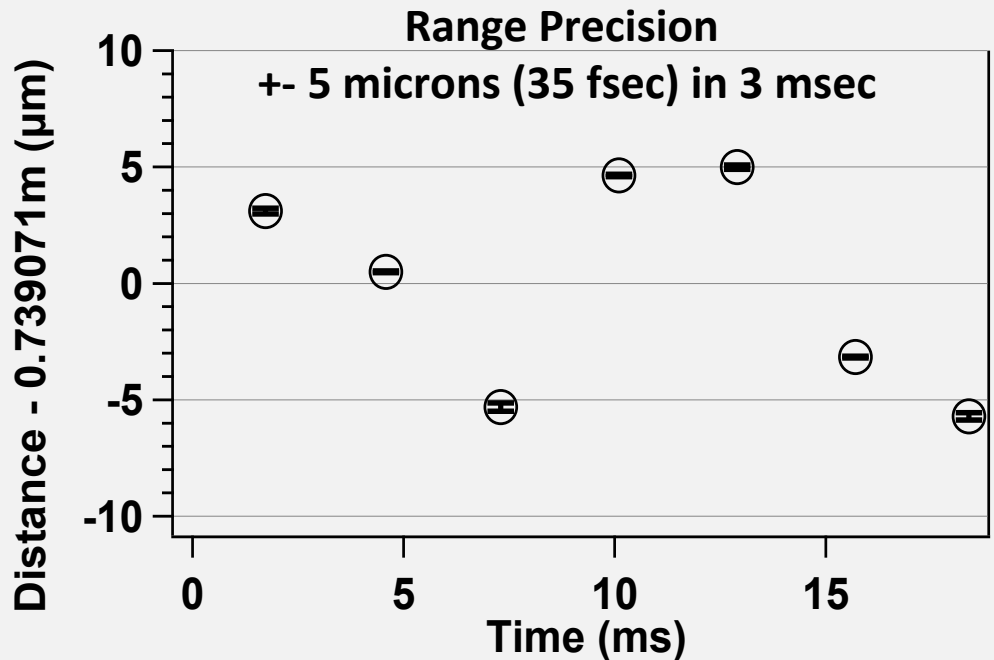
Accuracy \sim
30 kHz/ μ s
(1.5 MHz @ 20 ns)

FM CW Ranging Lab Demonstration

Preliminary Results



>10x faster should be possible



Conclusion

- **Combs used in many ways for ranging**
- **Direct Dual Comb Ranging system**
 - Phase-locked system: nanometer absolute ranging at a distance
 - Free-running system: sub-micron ranging in < 1 msec at distance
 - Multiplexed penalty compared to cw coherent laser radar
- **Comb-based metrology of swept lasers can track “arbitrary” cw laser waveforms**
 - Follow waveforms with chirps of few thousand THz/sec
 - Absolute or relative frequency measurements
- **Preliminary comb-assisted FMCW**
 - Processing intensive
 - Range resolution $\sim 1/\text{Bandwidth} \sim 1$ psec ~ 150 microns in 3 msec
 - Range precision of 5 microns in 3 msec
 - Potential 10x improvement in speed possible....